

# COLUMNS

DIFFERENTIAL EQUATION FOR ELASTIC CURVE:

$$EI \frac{d^2 V}{dx^2} = M_r = -PV \quad \rightarrow = k^2$$

$$\frac{d^2 V}{dx^2} + \frac{P}{EI} V = 0 \quad \text{SECOND ORDER HOMOGENEOUS DIFFERENTIAL EQUATION}$$

ASSUMED:  $V = A \sin kx + B \cos kx$

$$\left(-k^2 + \frac{P}{EI}\right) (A \sin kx + B \cos kx) = 0$$

BOUNDARY CONDITIONS:  $V = 0$  at  $x = 0$   
 $V = 0$  at  $x = L$

$$A \sin 0 + B \cos 0 = 0 \rightarrow B = 0$$

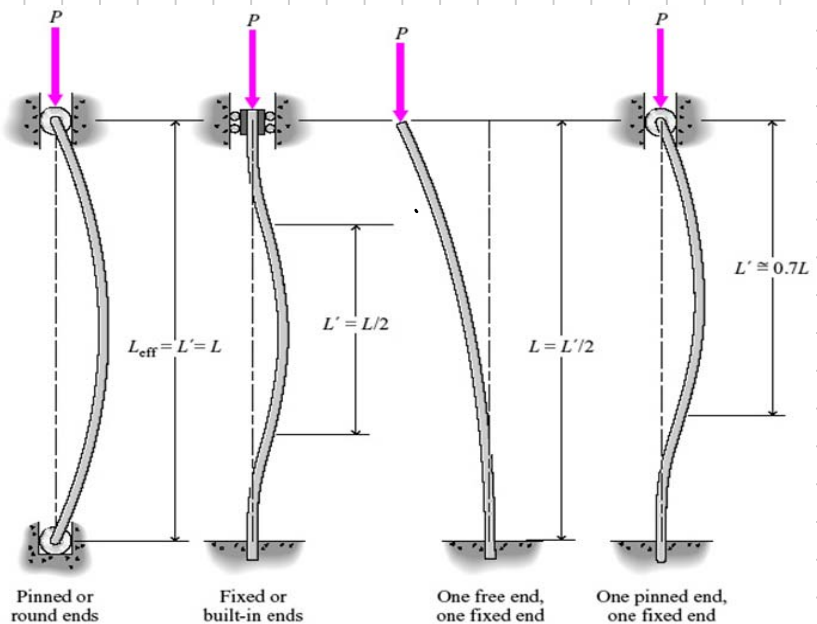
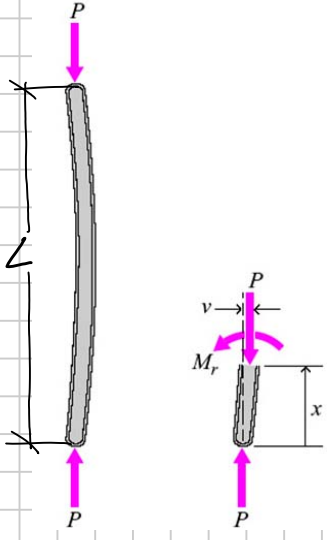
$$A \sin kL + B \cos kL = 0 \rightarrow A \sin kL = 0$$

$\neq 0 = 0$  for  $kL = n \cdot \pi$   
 with  $n = 1, 2, 3, \dots$

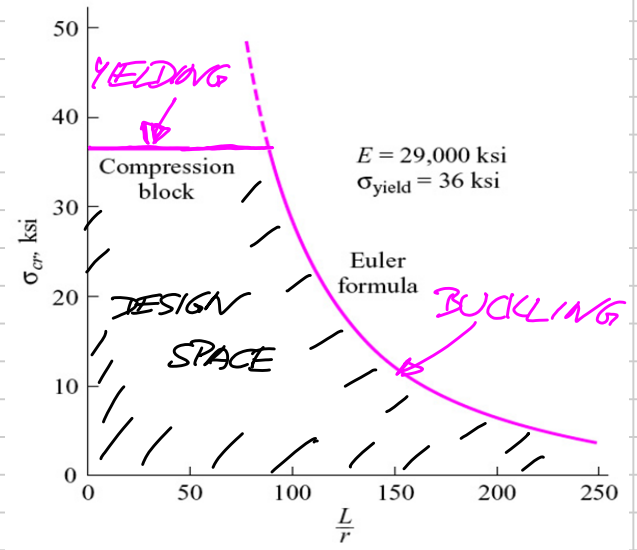
$$k \cdot L = \sqrt{\frac{P}{EI}} \cdot L = n\pi$$

$$P = \frac{n^2 \pi^2 EI}{L^2} \text{ with } n = 1, 2, 3, \dots$$

$$P_{crit} = \frac{\pi^2 EI}{L^2}$$



SHAPES AT ONSET OF BUCKLING



COLUMN LIMIT STATES